

# On the use of mutations to account for diversity in a multi-trait model of phytoplankton community

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# Simulating Plankton Evolution with Adaptive Dynamics (SPEAD)

## Objectives:

- Develop a marine ecosystem model that includes the adaptive evolution of phytoplanktonic organisms ...

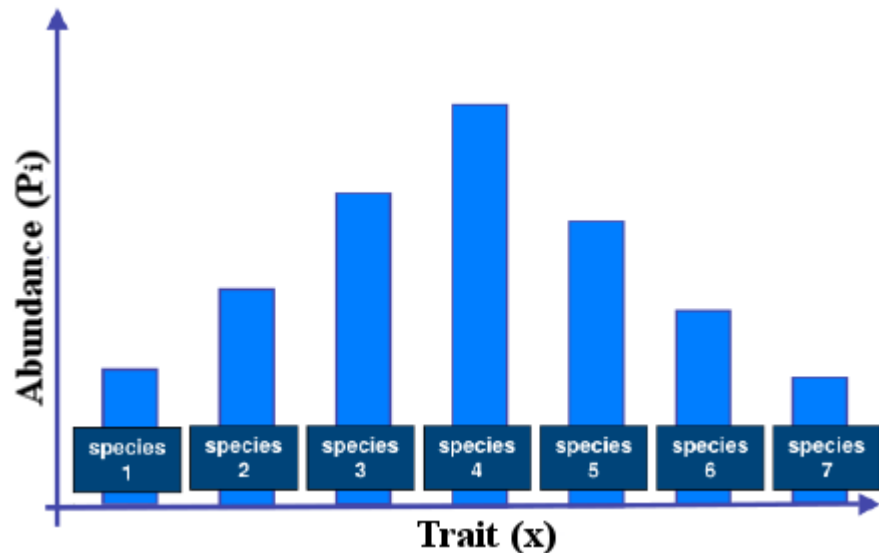
# Simulating Plankton Evolution with Adaptive Dynamics (SPEAD)

## Objectives:

- Develop a marine ecosystem model that includes the adaptive evolution of phytoplanktonic organisms ...
- ... in order to better predict the response of marine ecosystems to climate change scenarios

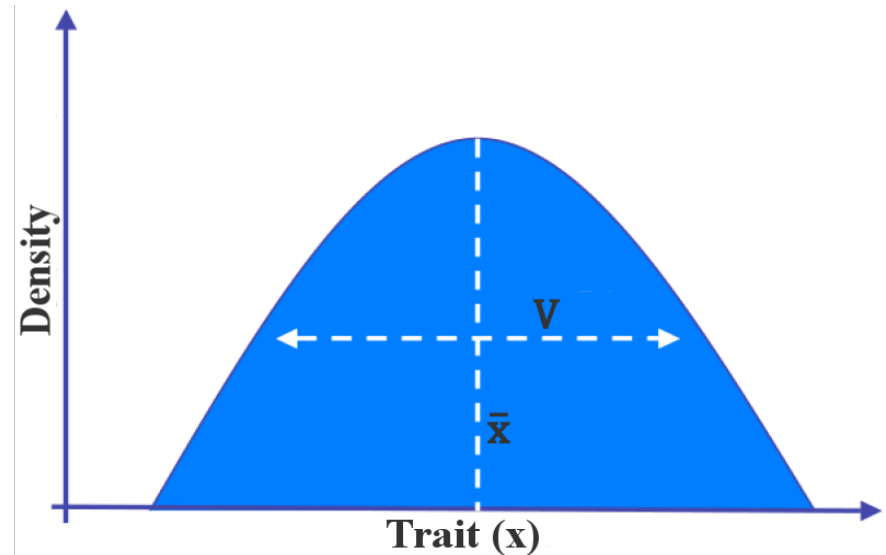
# Trait-based models

Traits are plankton characteristics affecting competition (size, optimal temperature, optimal irradiance, resistance to predation ...)



Multi-species model:

$$P_1, P_2 \dots P_n$$



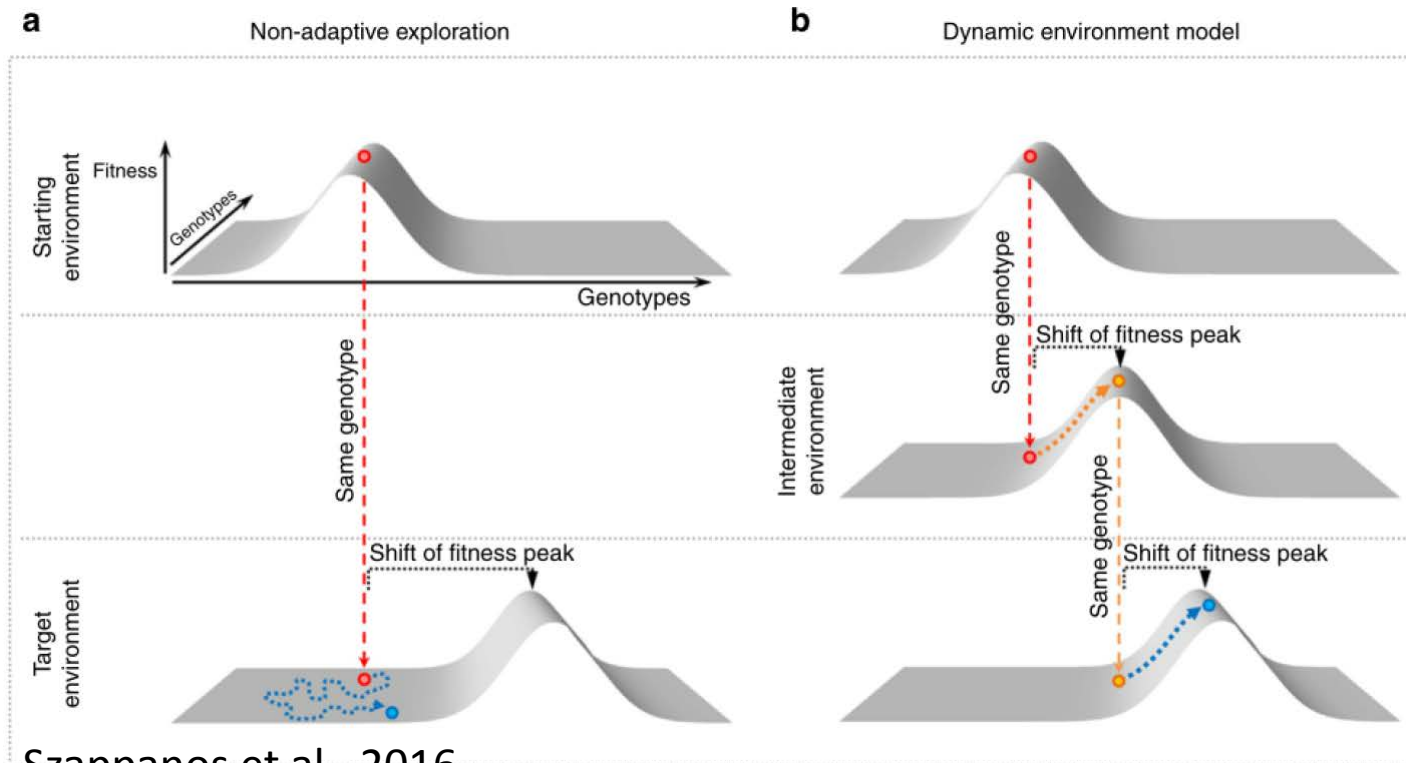
Aggregated model:

$$P_{tot}, \bar{x}, V$$

# Adaptive dynamics

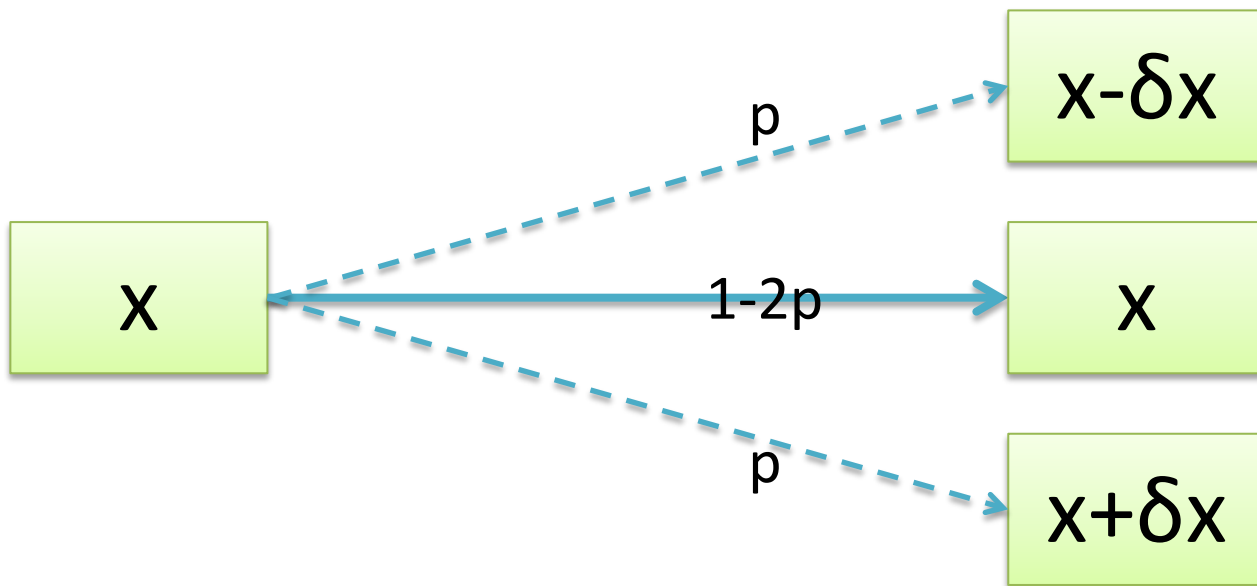
Mean trait moves to the value of highest fitness

➤ Requires biodiversity



# Trait diffusion (Merico et al., 2014)

The traits of offsprings can diverge from the traits of their parents, with a probability  $p$ .  $p = \frac{v}{(\delta x)^2}$  where  $v$  is a diffusivity parameter.

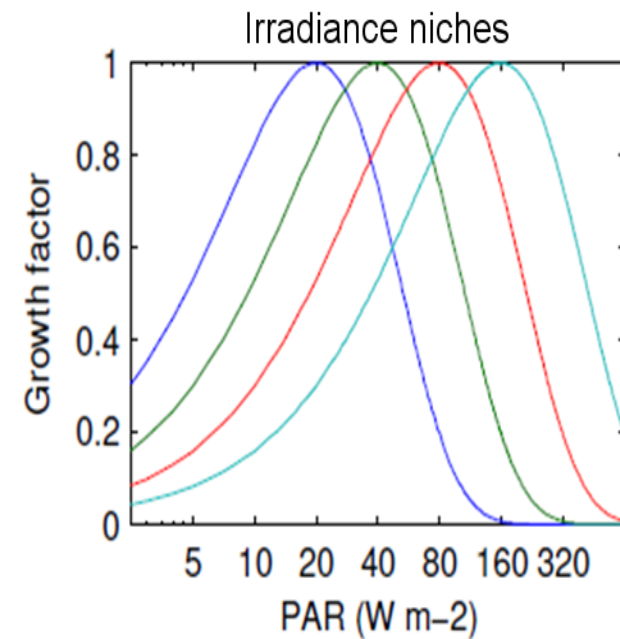
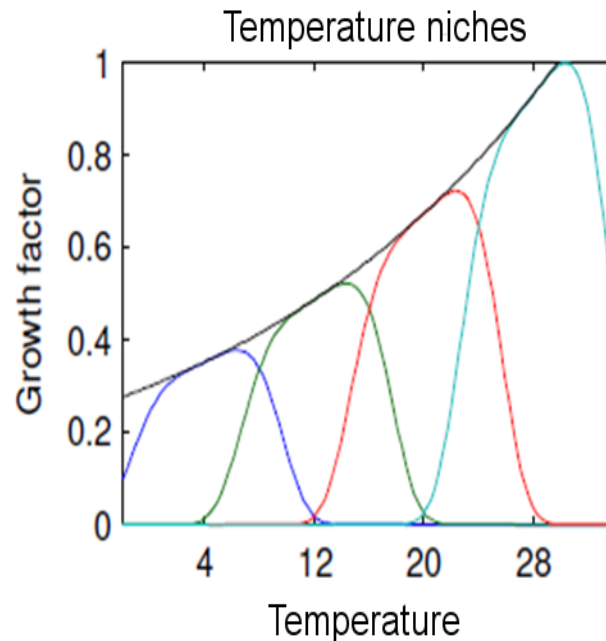
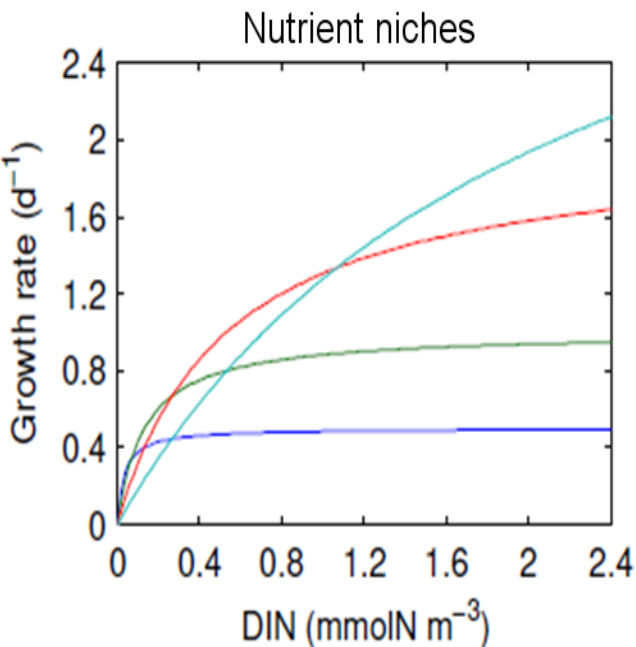


Represent all random and heritable mutations

# Traits and trade-offs

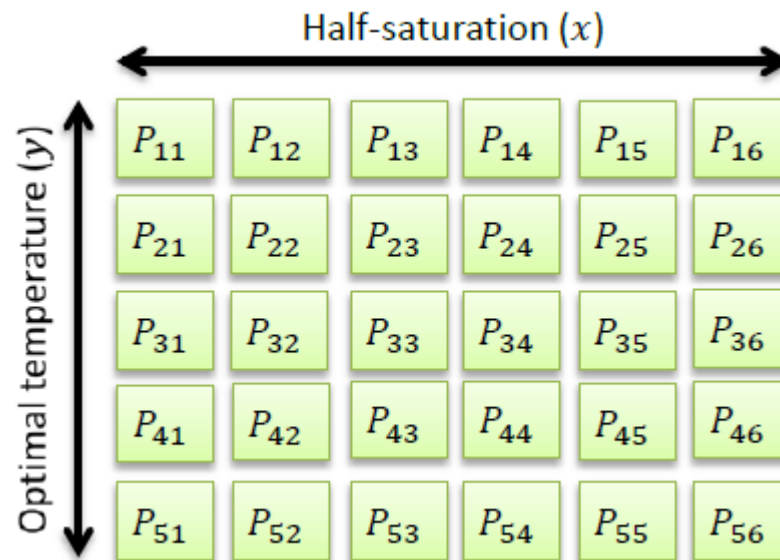
3 traits in the DARWIN model, 2 already included

- ✓ Affinity for Dissolved Inorganic Nitrogen, trade-off with maximum growth rate
- ✓ Optimum temperature ( $T_{opt}$ )
- Optimum irradiance ( $I_{opt}$ ) (yet to be included)



# Multi-species (discrete) model

$N_x * N_y$  species with  $N_x$  values of  $x$  and  $N_y$  values of  $y$

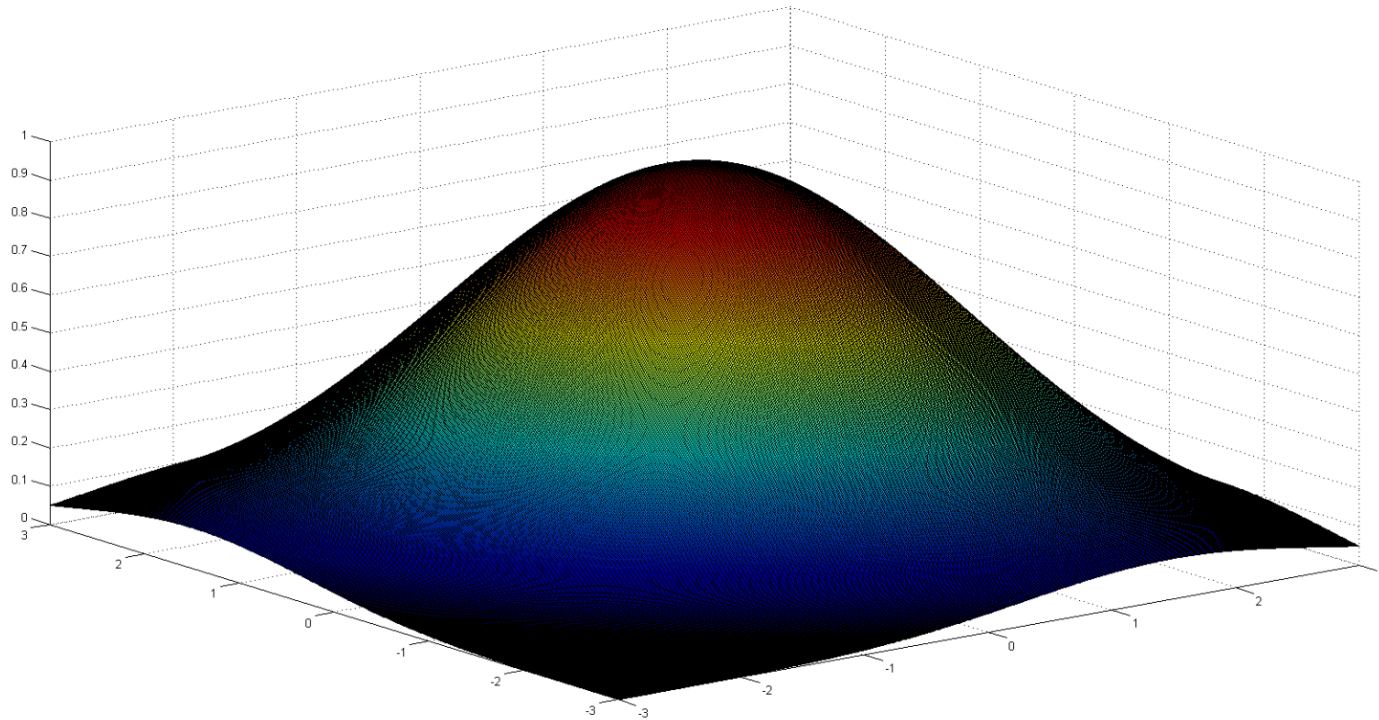


$N_x N_y$  differential equations  $\rightarrow$  Computationally expensive



# Aggregated (continuous) model

Bivariate normal distribution is assumed.



6 moments:  $P$ ,  $\bar{x}$ ,  $\bar{y}$ ,  $V_x$ ,  $V_y$  and  $C_{xy}$

3 diagnostic variables:  $\sigma_x = \sqrt{V_x}$ ,  $\sigma_y = \sqrt{V_y}$  and  $R_{xy} = \frac{C_{xy}}{\sigma_x \sigma_y}$

# Aggregated (continuous) model

Differential equations derived using the method of Norberg et al. (2001)

The net growth rate ( $a$ ) and the reproduction rate ( $r$ ) are Taylor-expanded to the order 2 around the mean trait values ( $\bar{x}$  and  $\bar{y}$ ):

$$a(x, y) = a(\bar{x}, \bar{y}) + \frac{\partial a}{\partial x}(x - \bar{x}) + \frac{\partial a}{\partial y}(y - \bar{y}) + \frac{1}{2} \frac{\partial^2 a}{\partial x^2}(x - \bar{x})^2 + \frac{1}{2} \frac{\partial^2 a}{\partial y^2}(y - \bar{y})^2 + \frac{\partial^2 a}{\partial x \partial y}(x - \bar{x})(y - \bar{y})$$

Equations of  $P$ ,  $\bar{x}$  and  $\bar{y}$  follow directly. They depend on  $a$ , its derivatives and the moments of the trait distribution ( $P$ ,  $\bar{x}$ ,  $\bar{y}$ ,  $V_x$ ,  $V_y$  and  $C_{xy}$ )

The equations on  $V_x$ ,  $V_y$  and  $C_{xy}$  depend on moments of higher order (3 and 4). We make a closure by assuming a normal distribution.

# Aggregated (continuous) model

$$\frac{dP}{dt} = P \left[ a + \frac{1}{2} V_x a_{xx} + C_{xy} a_{xy} + \frac{1}{2} V_y a_{yy} \right]$$

$$\frac{d\bar{x}}{dt} = V_x a_x + C_{xy} a_y$$

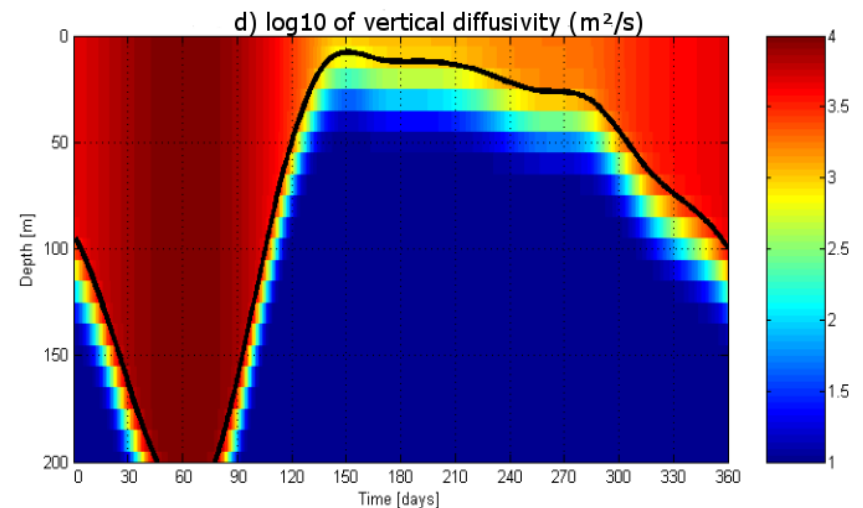
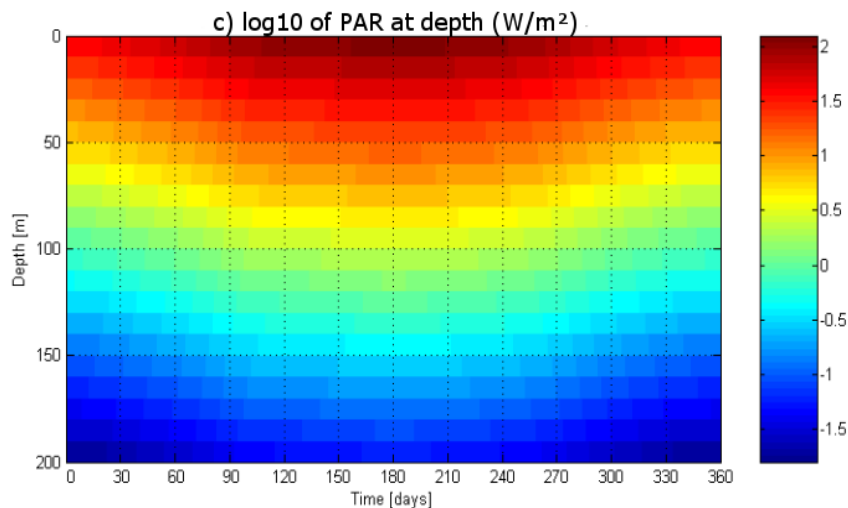
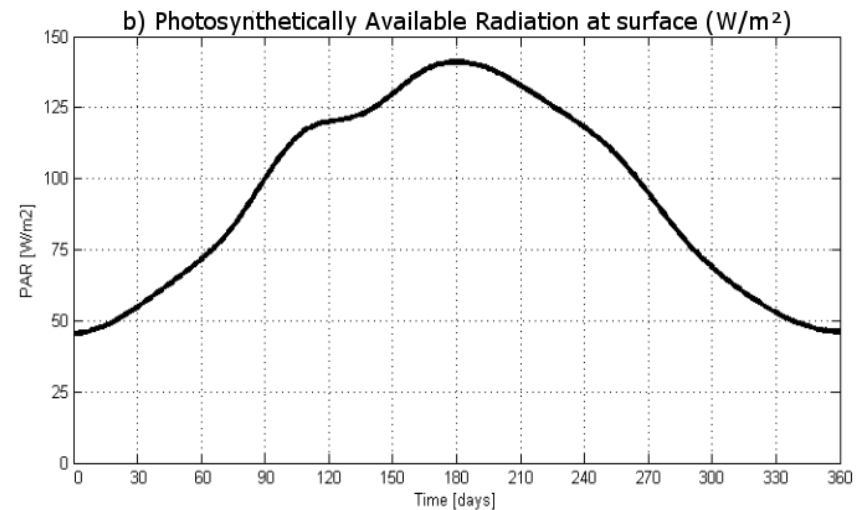
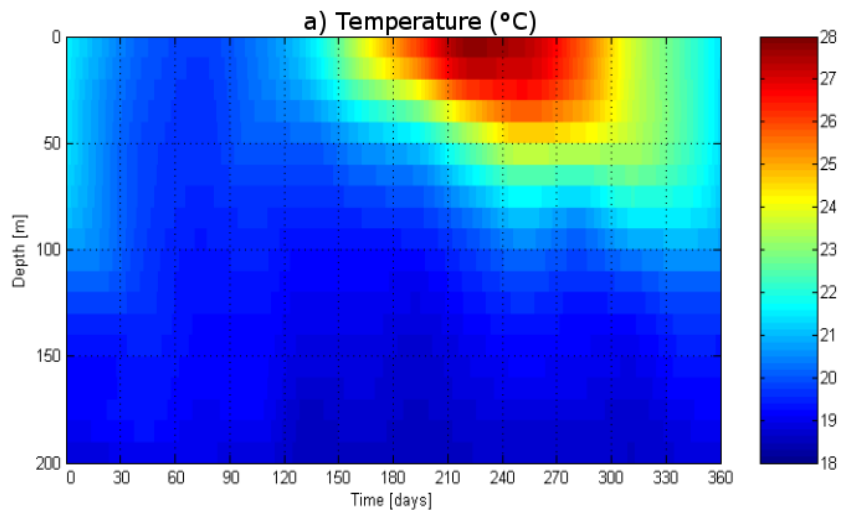
$$\frac{d\bar{y}}{dt} = C_{xy} a_x + V_y a_y$$

$$\frac{dV_x}{dt} = V_x^2 a_{xx} + 2V_x C_{xy} a_{xy} + C_{xy}^2 a_{yy} + 2v_x \left( r + \frac{1}{2} V_x r_{xx} + C_{xy} r_{xy} + \frac{1}{2} V_y r_{yy} \right)$$

$$\frac{dV_y}{dt} = C_{xy}^2 a_{xx} + 2V_y C_{xy} a_{xy} + V_y^2 a_{yy} + 2v_y \left( r + \frac{1}{2} V_x r_{xx} + C_{xy} r_{xy} + \frac{1}{2} V_y r_{yy} \right)$$

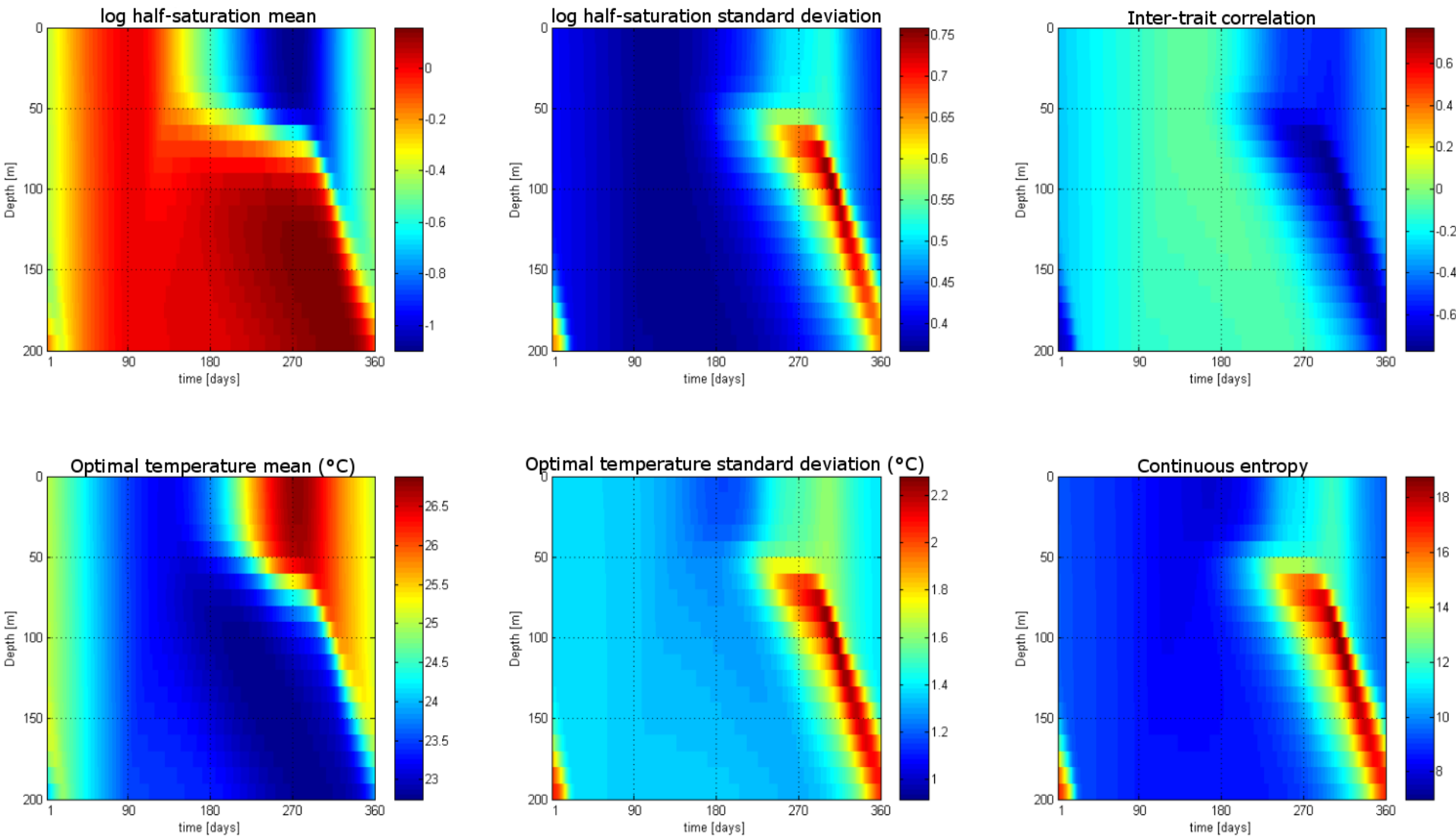
$$\frac{dC_{xy}}{dt} = V_x C_{xy} a_{xx} + (V_x V_y + C_{xy}^2) a_{xy} + C_{xy} V_y a_{yy}$$

# Forcings (from Sargasso Sea)



# Continuous model outputs

( $v_x = 0.002$  and  $v_y = 0.018$ )



# Simulating Plankton Evolution with Adaptive Dynamics in a global ocean model (SPEAD)

- ✓ Develop an aggregated phytoplankton model with two traits
  - Add optimal irradiance
  - Couple with a circulation model (MITGCM) and simulate future changes in phytoplankton communities at a global scale (invasion vs adaptation)